

Computer experiments & Stochastic Calculus with applications to PDE modeling



ECTS
3 crédits



Hourly volume

Introducing

Objectives

At the end of this module, the student will have understood and be able to explain (main concepts) the following.

Computer Experiment

- Metamodelling for optimization / uncertainty quantification of a computer code
- At least the two main families of metamodels : chaos polynomials and Gaussian processes
- Kernel customization to account for external knowledge
- Design of computer experiments
- Global sensitivity analysis

Stochastic calculus

- The brownian motion as well as the Wiener integral and Itô's formula
- The relationship between a stochastic differential equation and its Fokker-Planck equation.
- The rewriting of a parabolic or elliptical problem using a well-chosen stochastic process.

The student should be able:

Computer Experiments

- At a theoretical level, to do computations for:
 - covariance kernels and Gaussian process
 - ANOVA decomposition, Sobol indices
- At a practical level, to perform the complete methodology for analyzing a computer code

- design of experiments
 - metamodel construction / evaluation
 - application to optimization / uncertainty quantification of a computer code
- Stochastic calculus
- Derive simple models on noise filtration and stochastic control.
 - Numerically implement the resolution of a parabolic or elliptic equation using a particle-based probabilistic method.

Necessary prerequisites

Gaussian vectors. Probability. ODE. Basics of PDE.

Practical info

Location(s)

Toulouse