

## 4th YEAR MATHEMATICAL MODELING

### Practical info

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#### Location(s)

 Toulouse

# Partial Derivative Equations & Monte Carlo methods



ECTS  
4 crédits



Hourly volume  
53h

## Introducing

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### Objectives

At the end of this module, the student will have understood and be able to explain (main concepts):

PDE

- The four fundamentals PDE models, with their solution behaviors
- The Finite Difference discretization method

Monte-Carlo

- The fundamental principles of simulating random variables and Monte-Carlo methods.

The student will be able to:

PDE

- To model basic fundamental phenomena by employing PDE
- To derive a Finite Difference scheme (consistent, stable, convergent).

Monte-Carlo

- Simulate a random variable by different methods, use probabilistic, choose appropriate techniques for variance reduction and error estimation.

Basic numerical methods

Monte-Carlo

A basic course on probabilities.

## Practical info

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### Location(s)

 Toulouse

## Necessary prerequisites

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EDP

Differential calculus, analysis, ODE

# Advanced probability and Monte Carlo methods



ECTS  
4 crédits



Hourly volume  
53h

## Introducing

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### Objectives

Objectives:

At the end of this module, the student will have understood and be able to explain (main concepts):

- The notion of conditional expectation, the main properties of martingales and their classical use in modelling,
- Stochastic algorithms of Robbins-Monro type.
- The fundamental principles of simulating random variables and Monte-Carlo methods.

The student will be able to:

- To compute a conditional expectation, to show that a random process is a martingale, to use the various theorems (Doob, optional stopping and convergences), in particular for the maximum likelihood estimation.

- Build and study the convergence of stochastic optimization algorithms, apply these methods to different problems (quantile, quantization,  $\hat{\epsilon}$ )

Simulate a random variable by different methods, use probabilistic, choose appropriate techniques for variance reduction and error estimation

Necessary knowledge:

A basic course on probabilities.

### Practical info

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#### Location(s)

 Toulouse

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## Necessary prerequisites

## Improve your management abilities



ECTS

4 crédits



Hourly volume

45h

## Introducing

Management I3CCGE51

### Objectives

At the end of this module, the student will

¿ Know the legal environment and responsibilities of a business activity

¿ Be able to objectively assess the financial health of a company and evaluate the rentability of an investment

¿ Realize a market diagnosis (benchmarking) and a business diagnosis in order to make decisions and set goals and strategies

¿ Collect the market data and put in action a business plan adapted to the means and goals of the company  
Module L 2

The objectives, defined in reference to the CEFR for the 5 language activities, are specific for the language studied Chinese, German, Spanish ¿ and the level of the student.

They can be consulted on :

<https://moodle.insa-toulouse.fr/course/view.php?id=44>

In certain cases, students may be authorised to follow an English module instead of another language

## Practical info

### Location(s)

 Toulouse

## Necessary prerequisites

## Toulouse School of Management

### Practical info

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#### Location(s)

 Toulouse

## Optimisation II



ECTS  
4 crédits



Hourly volume  
54h

## Introducing

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### Objectives

At the end of this module, the student will have understood and be able to explain (main concepts):

- Deterministic differentiable optimisation :  
Existence and unicity of optimisation problems, KKT points, Convergence of optimization algorithm, Lagrangian duality
- Discrete stochastic optimisation :  
The Metropolis-Hastings algorithm, the simulated annealing algorithm, genetic algorithms.

The student will be able:

- To identify families of optimization problems
- To choose and implement suitable first and second order algorithms
- To implement a Metropolis-Hastings algorithm in order to simulate, approximately, a given discrete probability distribution on a huge finite space.
- To implement a simulated annealing algorithm in order to minimize a given function on a huge finite space.

## Practical info

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### Location(s)

 Toulouse

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## Necessary prerequisites

Optimisation I  
Markov chains and applications

# Signal Processing 1



ECTS  
4 crédits



Hourly volume  
43h

## Introducing

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### Objectives

At the end of this module, the student will have understood and be able to explain (main concepts):

- 1) Signal and Image processing basic notions : sampling, windowing and sampling
- 2) FFT algorithm
- 3) Basis notions on Hilbert spaces and Hilbert bases

The student will be able to:

- 1) Use the FFT and understand the output on a Signal or an image.
- 2) Apply several transformations to a signal and an image using the FFT

## Practical info

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### Location(s)



Toulouse

# Statistical Modelling



ECTS

4 crédits



Hourly volume

53h

## Introducing

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### Objectives

At the end of this module, the student will have understood and be able to explain (main concepts):

- The use of statistical tests for goodness-of-fit, independence, populations comparisons
- The characteristics of a linear model and a generalized linear model, and their use for statistical modelling

At the end of this module, the student should be able to:

- Choose a test procedure suited to a given problem
  - Build nonparametric test procedures to compare two populations
  - Build goodness-of-fit tests for a single distribution or a family of distributions
  - Choose a linear model or a generalized linear model suited to a given problem
  - Estimate the parameters in a linear model and a generalized linear model
  - Use statistical tests to validate or invalidate hypotheses on these linear models and generalized linear models.
  - Implement a variable selection strategy
  - Perform a complete statistical analysis on a real data set using a linear model or a generalized linear model
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## Necessary prerequisites

Probability and Statistics (I2MIMT31)  
Statistics (I3MIMT15)

## Practical info

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### Location(s)

 Toulouse



# HPC, Matrix Computations and Large Sparse Systems



ECTS  
4 crédits



Hourly volume  
59h

## Introducing

### Objectives

At the end of this module, the student will have understood and be able to explain (main concepts):

Eigenproblems :

- Different eigenproblems, their conditioning and Schur's factorization,
- Different methods for eigenvalue problems : power method, orthogonal iterations, QR method and Krylov subspace methods.

HPC :

This module is focused on the presentation of the basic mechanisms used to achieve high performance on modern computers. The language used by the students will be Python/C with which they'll learn to implement some MPI. They will also learn to program some Krylov's solvers as well as the LU factorization and to efficiently solve Poisson's equation discretized with finite differences.

Sparse systems :

- Principle and some strategies for sparse storages,
- Principle of different projection techniques to define iterative methods for solving sparse linear systems,
- Principle of different preconditioning techniques
- Principle of some reordering techniques to solve sparse linear systems with direct methods.

The student will be able to:  
Eigenproblems :

Understand the difficulties of a problem, and choose a method.

Paradigms and languages :

At the end of this module, students will be able to develop and to maintain Python / C software codes, to analyze applications performances and to supplement them with MPI/OpenMP directives in order to enable a parallel execution.

Sparse systems :

Chose one or a few methods adapted to a given linear system.

### Necessary prerequisites

- Precedent courses on the following subjects : linear algebra, numerical analysis.
- Knowledge of the imperative programming language main concepts (Python and C).

## Practical info

### Location(s)

Toulouse

## Quality, security, environment



ECTS

2 crédits



Hourly volume

35h

## Introducing

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### Objectives

At the end of this module, the student will have understood and be able to explain (main concepts):

- Mains concepts and tools for 'quality'
- The principles and stakes in the health and in the safety at work.
- The main concepts of the IT security.
- The importance of the environmental strategy in a company.

The student will be able to:

- Integrate the aspects of Quality, Security, Environment into the analysis of problems and the development of solutions.
- Be capable of taking into account the environmental stakes and applying the principles of the sustainable development.

## Practical info

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### Location(s)

 Toulouse

## Improving one's autonomy and building one's own professional project level 2 S7



ECTS  
4 crédits



Hourly volume  
46h

### Introducing

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- ¿ Enrich your professional network
- ¿ Set development axes, objectives and action plans

### Objectives

At the end of this module, the student will have understood and be able to explain (main concepts):

Physical and Sports Activities

The student will be able to:

to list the problems to be solved:

¿ Know the Physical and Sports Activity (rules, meaning, roles, etc.),

¿ Design the objective of the project.

to organize:

¿ Know the constraints, the resources, and the means available,

¿ Know how to choose and plan actions over time,

¿ Know how to get involved in the group and the project: know how to adapt, dare to stimulate action, know how to give up, propose, etc.

to regulate:

¿ Know how to observe,

¿ Know how to carry out a balance sheet,

¿ Know how to readjust the choices if necessary.

Individualized Professional Project

The student should be able to:

¿ Develop your professional vision and define a strategy.

¿ Customize, present and compare your project to professionals

### Necessary prerequisites

Learning outcomes 1st, 2nd, 3rd year.

### Practical info

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#### Location(s)

 Toulouse

## Political sciences semester 1



ECTS  
3 crédits



Hourly volume

## Practical info

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### Location(s)



Toulouse

## [FRANCAIS] Challenge – Formation ECIU



ECTS  
1 crédits



Hourly volume

## Practical info

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### Location(s)



Toulouse

## [FRANCAIS] Challenge – Formation ECIU



ECTS  
2 crédits



Hourly volume

## Practical info

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### Location(s)



Toulouse

## [FRANCAIS] Challenge – Formation ECIU



ECTS  
3 crédits



Hourly volume

## Practical info

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### Location(s)



Toulouse

## [FRANCAIS] Challenge – Formation ECIU



ECTS  
4 crédits



Hourly volume

## Practical info

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### Location(s)



Toulouse



## [FRANCAIS] Challenge – Formation ECIU



ECTS  
5 crédits



Hourly volume

## Practical info

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### Location(s)



Toulouse

# Finite Element Methods & Model Reductions



ECTS  
4 crédits



Hourly volume

## Introducing

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## Location(s)

 Toulouse

## Objectives

At the end of this course, the student will have understood and will be able to :

- Write the weak (variational) form of the classical PDE models (with the corresponding energy minimization in symmetric cases).
- Write and code a FE scheme (for linear and non-linear scalar models)
- Develop offline-online strategies to perform reduced basis models in real time (POD and Machine Learning based).
- Employ Finite Element libraries in Python, FEniCS (and FreeFEM++),

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## Necessary prerequisites

Fundamentals of PDE models and math. analysis,  
Numerical analysis.

## Practical info

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# Modeling and scientific computing in fluid and structural mechanics



ECTS  
4 crédits



Hourly volume  
55h

## Introducing

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Fundamentals in:  
Continuum mechanics  
Numerical analysis  
Partial derivative equations

## Objectives

At the end of this module, the student will have understood and be able to explain (main concepts):

The fundamentals of Mechanics for fluid and deformable solids, from a physical, mathematical and numerical point of view.

The student will be able to:

- Understand the physical meaning of the various terms used in fluid mechanics and elasticity models.
- Calculate exact solutions of simple problems and interpret them physically
- Evaluate orders of magnitude and know the physical meaning of the main dimensionless numbers
- Formulate and apply a finite volume method for numerically solving simple problems of fluid mechanics
- Formulate and solve the problem of elasticity by means of the finite element method.
- Use an industrial software to model and compute the elasticity problem in static as well as in dynamic.
- Write and implement a mixed formulation to couple different elastic domains and different numerical codes used as black-boxes.

## Practical info

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### Location(s)

Toulouse

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## Necessary prerequisites

## Data analysis



ECTS

4 crédits



Hourly volume

58h

## Introducing

### Objectives

At the end of this module, the student will have understood and be able to explain (main concepts):

- Data base organisation of R and Python data frames. Syntaxes R and Python languages. R and Python functions design, program and test.
- Statistical analyses of multidimensional data: dimension reduction and clustering with R and Python.
- Statistical interpretation of various graphical displays including the different kinds of factor analyses and clustering.

The student will be able to:

- Manage big data sets with R and Python.
- Lead exploratory data analyses of real big data. It includes univariate, bivariate and multivariate data analyses featuring PCA, MCA, FDA, NMF kmeans, mixture models, DBSCAN depending on data structures and analysis purposes;
- Detect relevant structures within complex data sets and compile insightful interpretations.

## Practical info

### Location(s)

 Toulouse

# Stochastic Processes: Time Series and Gaussian Processes



ECTS  
4 crédits



Hourly volume  
58h

## Introducing

### Objectives

At the end of this lecture, the student should have acquired the following skills, as well theoretically than practically with the R statistical Software and / or Python.

#### 1) Time series

- Estimate or eliminate the trend and/or the seasonality of a time series
- Study the stationnarity of a time series
- Calculate and estimate the autocorrelogram and the autocorrelograms (total and partial) of a stationary process
- Study and/or adjust an ARMA (or ARIMA) model on a stationary time series
- Carry an optimal linear forecast of an ARMA process

#### 2) Gaussian processes

- Know the fundamental properties of Gaussian processes
- Be able to characterize a Gaussian process through its covariance function
- Be able to use Gaussian Processes for modeling real life situations.

#### 1) Time series

Probability and Statistics (MIC2) I2MIMT31

Statistics (MIC3) I3MIMT05

Probability and Inferential Statistics (I4MMMT21)

#### 2) Gaussian processes

Advanced probabilities: martingales, stochastic algorithms and Montecarlo methods.

Markov chains.

Integration and probabilities.

## Practical info

### Location(s)

Toulouse

## Necessary prerequisites

## Signal II and Optimization



ECTS  
4 crédits



Hourly volume  
50h

### Introducing

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#### Objectives

At the end of this module, the student will have understood and be able to explain (main concepts):

- 1) Wavelet transform
- 2) Filter Banks with exact reconstruction
- 3) Properties of wavelets (localisation in space and frequency) and applications to the approximation of functions.
- 4) Notion of sub-gradient and proximal operator in convex analysis
- 5) Basic properties of proximal and Forward-Backward algorithms

The student will be able to:

- 1) Provide examples of wavelets
- 2) Carry out numerical approximation of images with wavelets.
- 3) Identify which convex problems can be solve using the previous algorithms and be able to implement these algorithms on simple cases

### Practical info

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#### Location(s)

 Toulouse

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### Necessary prerequisites

Signal 1  
Optimization 1 & 2

## Project Research – Innovation



ECTS  
8 crédits



Hourly volume  
55h

## Practical info

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### Location(s)



Toulouse

# Machine learning



ECTS

4 crédits



Hourly volume

52h

## Introducing

## Location(s)

 Toulouse

## Objectives

At the end of this module, the student will have understood and be able to explain (main concepts):

- Properties and limits of the main machine learning algorithms.
- Bias - variance trade-off, model selection.
- Algorithms for risk estimation: bootstrap, cross validation.
- Optimization and algorithmic implementations with R and Python (Scikit-learn) of the studied algorithms.
- Ethical and legal concepts of artificial intelligence.

The student will be able to:

- Analyse big data sets from various domains: insurance, marketing, industry, by using R and Python libraries.
- Execute the main machine learning methods and algorithms (discriminant analysis, k-nn, support vector machines, classification and regression trees, random forests, neural networks..)
- Optimize hyper-parameters values and construct pipelines for automating.
- Optimize the missing values management.
- Detect ethical or legal failures (bias, discrimination, opacity) of machine learning algorithms.

## Practical info



## Communication in organisations with LV2



ECTS

6 crédits



Hourly volume

### Introducing

#### Objectives

Objectives:

At the end of this module, the student will have understood and be able to explain (main concepts):

- How to answer the demand of the civil society for technical and scientific information
- How to carry out critical analysis in order to give appropriate answers when questioned about such issues
- How to consider the circulation and content of information within the organizations in which they will be hired

The classes given in English will focus on the specific linguistic characteristics of the English used in scientific contexts in order for the students to understand and master them.

The students will also be made aware of the specificities of scientific English as relates to publications in his specific field of research.

Module L 2

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In certain cases, students may be authorised to follow an English module instead of another language

#### Necessary prerequisites

Necessary knowledge:

For classes in English : understanding of scientific English

### Practical info

#### Location(s)



Toulouse

## Political sciences semestre 2



ECTS  
3 crédits



Hourly volume

## Practical info

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### Location(s)



Toulouse

## [FRANCAIS] Challenge – Formation ECIU



ECTS  
1 crédits



Hourly volume

## Practical info

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### Location(s)



Toulouse

## [FRANCAIS] Challenge – Formation ECIU



ECTS  
2 crédits



Hourly volume

## Practical info

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### Location(s)



Toulouse

## [FRANCAIS] Challenge – Formation ECIU



ECTS  
3 crédits



Hourly volume

## Practical info

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### Location(s)



Toulouse

## [FRANCAIS] Challenge – Formation ECIU



ECTS  
4 crédits



Hourly volume

## Practical info

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### Location(s)



Toulouse

## [FRANCAIS] Challenge – Formation ECIU



ECTS  
5 crédits



Hourly volume

## Practical info

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### Location(s)



Toulouse